



Schema Mapping Discovery from Data Instances

Georg Gottlob, Pierre Senellart



Different sources organize the same data differently

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Different sources organize the same data differently

[Querying websites using compact skeletons - all 11 versions »](#)

A Rajaraman, **JD Ullman** - Journal of Computer and System Sciences, 2003 - Elsevier

Several commercial applications, such as online comparison shopping and process automation, require integrating information that is scattered across multiple websites or XML documents. Much research has been devoted to this problem, ...

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[BOOK] Wprowadzenie do teorii automatów, języków i obliczeń

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[Improving the efficiency of database-system teaching - all 3 versions »](#)

JD Ullman - Proceedings of the 2003 ACM SIGMOD international conference ..., 2003 - portal.acm.org

ABSTRACT The education industry has a very poor record of productivity gains.

In this brief article, I outline some of the ways the teaching of a college course in database systems could be made more efficient, and student time used ...

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[A survey of new directions in database systems - all 5 versions »](#)

JD Ullman - Database Systems for Advanced Applications, 2003.(DASFAA ..., 2003 - ieexplore.ieee.org

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Motivation

Context

- Multiple data sources containing information about **similar entities**, with some **redundancy** (e.g., sources of the deep Web).
- Several different ways to present this information, i.e., several **different schemata**.
- No **a priori** information about (some of) these schemata.

How to know the **relationships** between these schemata, by just looking at the instances?

Other way to see this problem: **Match** operator on schema mappings, in the setting of **data exchange**.



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Problem definition

Problem

Given two (relational) database instances I and J with different schemata, what is the **optimal** description Σ of J knowing I (with Σ a finite set of formulas in some logical language)?

What does optimal implies:

- **Conciseness** of description.
- **Validity** of facts predicted by I and Σ .
- All facts of J **explained** by I and Σ .

(Note the asymmetry between I and J ; context of **data exchange** where J is computed from I and Σ).



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Introduction

TGDs, Cost, Optimality

TGDs

Cost and Optimality

Results

Extensions, Variants

Conclusion

Definition (Source-to-target tgd)

First-order formula of the form:

$$\forall \mathbf{x} \varphi(\mathbf{x}) \rightarrow \exists \mathbf{y} \psi(\mathbf{x}, \mathbf{y})$$

with:

- φ conjunction of source relation atoms;
- ψ conjunction of target relation atoms;
- all variables of \mathbf{x} bound in φ .

Example

$$\forall x_1 \forall x_2 R_1(x_1, x_2) \wedge R_2(x_2) \rightarrow \exists y R'(x_1, y)$$



Particular tgds

Two ways of having **simpler** tgds:

- Disallow existential quantifiers on the right hand-side: **full tgds**.
- Disallow cycles on both left- and right-hand sides: **acyclic tgds**.
(Classical notion of acyclicity on hypergraphs extending the basic notion of acyclicity on graphs.)

Examples

$\forall x_1 \forall x_2 \forall x_3 R_1(x_1, x_2) \wedge R_2(x_2, x_3) \wedge R_3(x_3, x_1) \rightarrow R'(x_1)$ is **cyclic** (and full).

$\forall x_1 \forall x_2 \forall x_3 R_1(x_1, x_2) \wedge R_2(x_2, x_3) \rightarrow R'(x_1)$ is **acyclic** (and full).

\mathcal{L}_{tgd} : arbitrary source-to-target tgds;

$\mathcal{L}_{\text{full}}$: full tgds;

$\mathcal{L}_{\text{acyc}}$: acyclic tgds;

$\mathcal{L}_{\text{facyc}}$: full and acyclic tgds.



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Pertinence of a set of tgds

Example

R	R'
a	a
b	b
c	a
d	d
	g
	h

$$\Sigma_0 = \emptyset$$

$$\Sigma_1 = \{\forall x R(x) \rightarrow R'(x, x)\}$$

$$\Sigma_2 = \{\forall x R(x) \rightarrow \exists y R'(x, y)\}$$

$$\Sigma_3 = \{\forall x_1 \forall x_2 R(x_1) \wedge R(x_2) \rightarrow R'(x_1, x_2)\}$$

$$\Sigma_4 = \{\exists y_1 \exists y_2 R'(y_1, y_2)\}$$



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- Size of a formula: **number of occurrences of variables** and constants.
- **Cost** of a schema mapping Σ : Size of the **minimum repair** of Σ that is valid and explains all facts of J .
- Types of repairs considered:
 - “**fix**” a universal quantifier by adding conditions ($x = a$ or $x \neq a$);
 - “**fix**” an existential quantifier by giving corresponding constants ($\tau(x) \rightarrow y = a$ with τ a conjunction of conditions on universally quantified variables);
 - add **ground facts** to the target instance.
- The problem is then to find a schema mapping of **minimal cost**.



Example cost computation

Example

R
a
b
c
d

R'	
a	a
b	b
c	a
d	d
g	h

$$\forall x R(x) \rightarrow R'(x, x)$$

Predicted R'

a	a
b	b
c	c
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Example cost computation

Example

R
a
b
c
d

R'
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b b
c a
d d
g h

$$\forall x R(x) \wedge x \neq c \rightarrow R'(x, x)$$

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Example cost computation

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R
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$$R'(c, a)$$

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a
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R'
a a
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c a
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$$\forall x R(x) \wedge x \neq c \rightarrow R'(x, x)$$

$$R'(c, a)$$

$$R'(g, h)$$

Predicted R'

a	a
b	b
c	c
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Example cost computation

Example

R
a
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c
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R'
a a
b b
c a
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g h

$$\forall x R(x) \wedge x \neq c \rightarrow R'(x, x)$$

$$\exists y_1 \exists y_2 R'(y_1, y_2) \wedge y_1 = c \wedge y_2 = a$$

$$\exists y_1 \exists y_2 R'(y_1, y_2) \wedge y_1 = g \wedge y_2 = h$$

Predicted R'

a	a
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Cost: 17

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Problems considered

Decision problems of interest:

Cost: Is the cost of a given schema mapping less than K ?

Optimality: Is a given schema mapping optimal?

Complexity? Algorithms?



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Outline

Introduction

TGDs, Cost, Optimality

Results

Justification

Complexity Analysis

Extensions, Variants

Conclusion



Behavior for simple operators

Consider the **elementary operators** of the relational algebra:

- Projection
- Intersection
- Selection (conjunction of atomic conditions)
- Cross Product
- Join (on a given attribute)

Theorem

*For any elementary operator γ , the **tg**d naturally associated with γ is optimal with respect to $(I, \gamma(I))$ (or $(\gamma(J), J)$), under some basic assumptions.*



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Examples of naturally associated tgds

Examples

	Condition	I and J	Optimal tgd
Projection	$I \neq \emptyset$ $\pi_1(J) \cap \pi_2(J) = \emptyset,$ $ \pi_1(J) \geq 2$	$J = \pi_1(I)$ $I = \pi_1(J)$	$R(x, y) \rightarrow R'(x)$ $R(x) \rightarrow \exists y R'(x, y)$
Selection	$ \sigma_\varphi(I) \geq \frac{\text{size}(\varphi)+2}{3}$ $\sigma_\varphi(J) \neq \emptyset$	$J = \sigma_\varphi(I)$ $I = \sigma_\varphi(J)$	$R(x) \rightarrow R'(x)$ $R(x) \rightarrow R'(x)$
Product	$R_1^I \neq \emptyset, R_2^I \neq \emptyset$ $R_1^J \neq \emptyset, R_2^J \neq \emptyset$	$J = R_1^I \times R_2^I$ $I = R_1^J \times R_2^J$	$R_1(x) \wedge R_2(y) \rightarrow R'(x, y)$ $R(x, y) \rightarrow R_1'(x) \wedge R_2'(y)$



The Polynomial Hierarchy

P	polynomial deterministic algorithm
NP	polynomial non-deterministic algorithm
coNP	complement NP
DP	problems expressible as the conjunction of a NP and a coNP problem
Σ_2^P	polynomial non-deterministic with Σ_1^P oracle
Π_2^P	complement Σ_2^P
Σ_{n+1}^P	polynomial non-deterministic with Σ_n^P oracle
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Union of all these classes: $\text{PH} \subseteq \text{PSPACE}$, the polynomial hierarchy.



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(Combined) Complexity Results

	\mathcal{L}_{tgd}	$\mathcal{L}_{\text{full}}$
Cost	Σ_3^P, Π_2^P -hard	$\Sigma_2^P, \text{DP-hard}$
Optimality	$\Pi_4^P, \text{DP-hard}$	$\Pi_3^P, \text{DP-hard}$

	$\mathcal{L}_{\text{acyc}}$	$\mathcal{L}_{\text{facyc}}$
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Vertex-Cover in r -partite r -uniform hypergraph

Vertex-Cover: find a set of vertices of minimal size that cover all (hyper)edges in a (hyper)graph.

- **NP-complete** for general (hyper)graphs.
- **P**TIME for bipartite graphs (Kőnig's theorem).

Lemma

Vertex-Cover is NP-complete for r -partite r -uniform hypergraphs for $r \geq 3$.

r -partite: partition of the set of vertices into r sets, with no hyperedge spanning two vertices of the same set.

r -uniform: every hyperedge spans r vertices.



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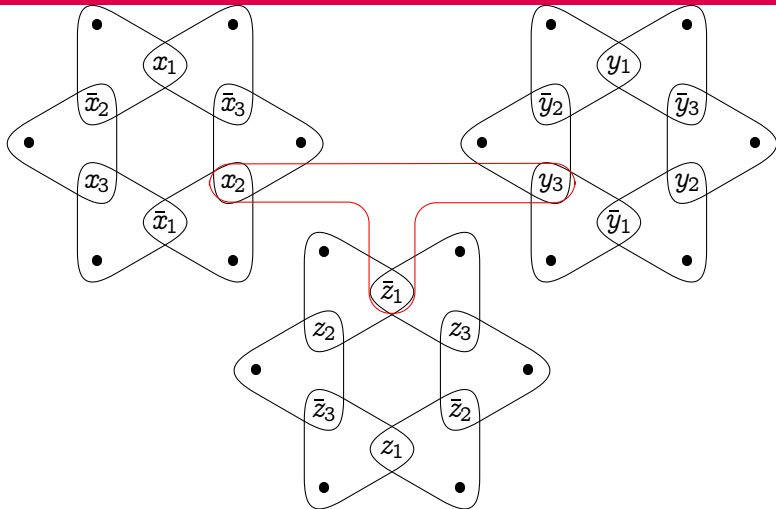
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r -uniform: every hyperedge spans r vertices.



Encoding of 3-SAT



$$\neg z \vee x \vee y$$



Cost is NP-hard for $\mathcal{L}_{\text{facyc}}$

Reduction from Vertex-Cover in 3-partite 3-uniform hypergraphs.

Without $x = a$ repairs on the left-hand side of a tgd:

- $R(x_1, x_2, x_3) \rightarrow R'(x_1)$
- Source instance: **hypergraph**
- Target instance: **empty**

Cost: size of the tgd plus **twice the minimum size of a vertex cover**.

With $x = a$ repairs: a little more difficult, but feasible!



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Relational Calculus

Other Cost Functions

Conclusion



Extension to Relational Calculus

- Definition of repairs can be extended to relational calculus.
- Same definition of cost, optimality.
- Cost is **not recursive** (but co-r.e.).
- Computability of **Optimality**: **open** (!).



Other Cost Functions

Why not counting the number of tuples to add or remove in J ?

... because it can be **exponential** in the size of the schema mapping!

Why not counting the number of tuples to add or remove in I or J ?

... because **selections are not captured!**



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In summary...

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- **High complexity** (up to fourth level of **PH**).



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- Link with **Inductive Logic Programming?**
- Heuristics?
- Approximation algorithms?
- Generalization of acyclicity?

Merci.

Wabdam